# The Phase Relations in the $\mathbf{I n}_{2} \mathbf{O}_{\mathbf{3}}-\mathrm{Fe}_{\mathbf{2}} \mathrm{ZnO}_{\mathbf{4}} \mathbf{-} \mathbf{Z n O}$ System at $1350^{\circ} \mathrm{C}$ 

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#### Abstract

The phase relations in the $\mathrm{In}_{2} \mathrm{O}_{3}-\mathrm{Fe}_{2} \mathrm{ZnO}_{4}-\mathrm{ZnO}$ system at $1350^{\circ} \mathrm{C}$ are determined by means of a classical quenching method. There are a series of homologous solid solutions, $\mathbf{l n}_{1.28} \mathrm{Fe}_{0.72} \mathrm{O}_{3}(\mathrm{ZnO})$ $\operatorname{InFeO} 3(\mathrm{ZnO}), \quad \mathrm{In}_{1.69} \mathrm{Fe}_{0.31} \mathrm{O}_{3}(\mathrm{ZnO})_{2}-\mathrm{InFeO}_{3}(\mathrm{ZnO})_{2}-\mathrm{In}_{0.85} \mathrm{Fe}_{1.15} \mathrm{O}_{3}\left(\mathrm{ZnO}_{2}, \quad \mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{3}-\mathrm{InFeO}_{3}(\mathrm{ZnO})_{3}-\right.$ $\mathrm{In}_{0.78} \mathrm{Fe}_{1.22} \mathrm{O}_{3}(\mathrm{ZnO})_{3}, \quad \mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{4}-\mathrm{InFeO}_{3}(\mathrm{ZnO})_{4}-\mathrm{In}_{0.62} \mathrm{Fe}_{1.38} \mathrm{O}_{3}(\mathrm{ZnO})_{4}, \quad \mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{5}-\mathrm{InFeO}_{3}(\mathrm{ZnO})_{5}-$ $\mathrm{In}_{0.67} \mathrm{Fe}_{1.33} \mathrm{O}_{3}(\mathrm{ZnO})_{5}, \quad \mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{6}-\mathrm{InFeO}_{3}(\mathrm{ZnO})_{6}-\mathrm{In}_{0.60} \mathrm{Fe}_{1.40} \mathrm{O}_{3}(\mathrm{ZnO})_{6}, \quad \mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{7}-\mathrm{InFeO}{ }_{3}(\mathrm{ZnO})_{7}-$ $\mathrm{In}_{0.51} \mathrm{Fe}_{1,49} \mathrm{O}_{3}(\mathrm{ZnO})_{7}, \mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{8}-\mathrm{InFeO}_{3}(\mathrm{ZnO})_{8}-\mathrm{In}_{1-x} \mathrm{Fe}_{1+x} \mathrm{O}_{3}(\mathrm{ZnO})_{8}(0.44 \leqq x \leqq 0.64), \mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{9}-$ $\operatorname{InFeO})_{3}(\mathrm{ZnO})_{9}-\mathrm{In}_{0.20} \mathrm{Fe}_{1.80} \mathrm{O}_{3}(\mathrm{ZnO})_{9}, \mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{10}-\mathrm{InFeO}_{3}(\mathrm{ZnO})_{10}-\mathrm{In}_{t-x} \mathrm{Fe}_{1+x} \mathrm{O}_{3}(\mathrm{ZnO})_{10}(0.74 \leqq x \leqq$ $0.89), \ln _{2} \mathrm{O}_{3}(\mathrm{ZnO})_{11}-\operatorname{InFeO} 3_{3}(\mathrm{ZnO})_{11}-\mathrm{In}_{1-x} \mathrm{Fe}_{1+x} \mathrm{O}_{3}(\mathrm{ZnO})_{11}(0.60 \leqq x<1.00)$, and $\mathrm{In}_{2} \mathrm{O}_{3}\left(\mathrm{ZnO}_{13}-\mathrm{InFeO}{ }_{3}\right.$ $(\mathrm{ZnO})_{13}-\mathrm{Fe}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{13}$ having the layered structures with space group $R \overline{3} m$ ( $m=$ odd ) or $P 6_{3} / m m c$ ( $m$ $=$ even) for $m$ in the $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{m}$. We conclude that there are a series of homologous phases, $\left(\mathrm{Fe}_{2} \mathrm{O}_{3}\right)(\mathrm{ZnO})_{m}(m \geqq 12)$, in the binary $\mathrm{ZnO}-\mathrm{Fe}_{2} \mathrm{O}_{3}$ system. The lattice constants for these solid solutions are presented as a hexagonal crystal system. It is also concluded that the crystal structures for each solid solution consist of three kinds of layers which are stacked perpendicular to the $c$-axis in the hexagonal crystal system. $\mathrm{In}_{1+x} \mathrm{Fe}_{1-x} \mathrm{O}_{3}(\mathrm{ZnO})_{m}(0 \leqq x \leqq 1)$ is composed of the $\mathrm{InO}_{15},\left(\mathrm{In}_{x} \mathrm{Fe}_{\mathrm{I}-x}\right.$ $\mathrm{Zn}) \mathrm{O}_{2.5}$, and ZnO layers, and $\mathrm{In}_{\mathrm{i}-x} \mathrm{Fe}_{1+x} \mathrm{O}_{3}(\mathrm{ZnO})_{m}(0 \leqq x \leqq 1)$ is composed of $\left(\mathrm{ln}_{1-x} \mathrm{Fe}_{x}\right) \mathrm{O}_{1.5}$, $(\mathrm{FeZn}) \mathrm{O}_{2.5}$, and ZnO layers, respectively. The solid solution range between $\mathrm{Fe}_{2} \mathrm{ZnO}_{4}$ and $\mathbf{l n}_{x} \mathrm{Fe}_{2-x} \mathrm{ZnO}_{4}$ ( $x=0.40 \pm 0.02$ ) with a spinel structure is observed. © 1990 Academic Press, Inc.


## Introduction

It may be interesting to analyze the relation between crystal structures of complex inorganic compounds and their constituent cations. In previous papers (1, 2), we presented the phase relations in the $\mathrm{In}_{2} \mathrm{O}_{3}-$ $\mathrm{Fe}_{2} \mathrm{O}_{3}-\mathrm{CuO}$ system at $1000^{\circ} \mathrm{C}, \quad \mathrm{In}_{2} \mathrm{O}_{3}-$ $\mathrm{Ga}_{2} \mathrm{O}_{3}-\mathrm{CuO}$ system at $1000^{\circ} \mathrm{C}$, $\mathrm{In}_{2} \mathrm{O}_{3}-\mathrm{Fe}_{2} \mathrm{O}_{3}-\mathrm{CoO}$ system at $1300^{\circ} \mathrm{C}$, $\mathrm{In}_{2} \mathrm{O}_{3}-\mathrm{Ga}_{2} \mathrm{O}_{3}-\mathrm{CoO}$ system at $1300^{\circ} \mathrm{C}$, and $\mathrm{In}_{2} \mathrm{O}_{3}-\mathrm{Fe}_{2} \mathrm{MgO}_{4}-\mathrm{MgO}$ system at $1300^{\circ} \mathrm{C}$, which were determined by means of a classical quenching method, and showed (In

[^0]$\left.\mathrm{FeO}_{3}\right)_{n} \mathrm{CuO}(n=1,2$, and 3) and (In $\left.\mathrm{GaO}_{3}\right)_{n} \mathrm{CuO}$ ( $n=1$ and 2) having ( Yb $\left.\mathrm{FeO}_{3}\right)_{n} \mathrm{FeO}$ structures (3-5), and both In $\mathrm{FeO}_{3}(\mathrm{CoO})$ and $\mathrm{InFeO}_{3}(\mathrm{MgO})$ having spinel structure (1, 2). Kasper prepared $\mathrm{In}_{2} \mathrm{O}_{3}$ $(\mathrm{ZnO})_{m}(m=2-5$, and 7$)$ in the $\mathrm{In}_{2} \mathrm{O}_{3}-\mathrm{ZnO}$ system at $1050-1550^{\circ} \mathrm{C}$, and reported their conditions of synthesis and the lattice constants as those in a hexagonal system (6). Cannard and Tilley (7) observed $\mathrm{In}_{2} \mathrm{O}_{3}$ $(\mathrm{ZnO})_{m}(m=4-7,9$, and 11) by high resolution electron microscopy and concluded from their lattice images for each phase that the structures of $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{m}$ are composed of both the $\mathrm{InO}_{1.5}$ and ZnO layers. In the $R_{2} \mathrm{O}_{3}-\mathrm{M}_{2} \mathrm{O}_{3}-\mathrm{ZnO}$ system at elevated
temperatures, $R \mathrm{MO}_{3}(\mathrm{ZnO})_{m}(R=\mathrm{Sc}$ and $\mathrm{In} ; M=\mathrm{Fe}, \mathrm{Ga}$, and Al ) having layered structures with space groups $R \overline{3} m$ ( $m=$ odd) or $P 6_{3} / m m c$ ( $m=$ even) were synthesized and the crystal structural models for each compound composed of $R \mathrm{O}_{1.5}$, $(M \mathrm{Zn}) \mathrm{O}_{2.5}$, and ZnO layers were presented by Kimizuka et al. (8). $R M \mathrm{O}_{3}(\mathrm{ZnO})$ is isostructural with $\mathrm{YbFe}_{2} \mathrm{O}_{4}$ (3). $R^{\prime} M \mathrm{O}_{3}(\mathrm{ZnO})_{m}$ ( $R^{\prime}=\mathrm{Lu}, \mathrm{Yb}, \mathrm{Tm}, \mathrm{Er}, \mathrm{Ho}$, and Y) and $R^{\prime} M \mathrm{O}_{3}\left(M^{\prime} \mathrm{O}\right)_{m}\left(R^{\prime}=\mathrm{Sc}, \mathrm{In}, \mathrm{Lu}, \mathrm{Yb}, \mathrm{Tm}\right.$, Ho, Er, and $\mathrm{Y} ; M=\mathrm{Fe}, \mathrm{Ga}$ and $\mathrm{Al} ; M^{\prime}=$ $\mathrm{Mg}, \mathrm{Mn}, \mathrm{Co}$, and $\mathrm{Fe}(\mathrm{II})$ ) which were isostructural with $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{m}$ were reported by Kimizuka and Mohri (9) and Kimizuka et al. (2), respectively. In the present paper, we report the phase relations in the $\mathrm{In}_{2} \mathrm{O}_{3}-\mathrm{Fe}_{2} \mathrm{ZnO}_{4}-\mathrm{ZnO}$ system at $1350^{\circ} \mathrm{C}$ which were determined by means of a classical quenching method, and show a series of homologous solid solutions which are isostructural with $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{m}$. The $\mathrm{In}_{1+x} \mathrm{Fe}_{1-x} \mathrm{O}_{3}(\mathrm{ZnO})_{m}$ structure (the value of $x$ for each $m$ is given in the fifth column of Table II) is interpreted as the stacking of $Z$ * $1 \mathrm{InO}_{1.5}, Z * 1\left(\mathrm{In}_{x} \mathrm{Fe}_{1-.} \mathrm{Zn}\right) \mathrm{O}_{2.5}$, and $Z *$ ( $m-1$ ) ZnO layers perpendicular to the $c$ axis in the unit cell ( $Z$ is the molecular number in the unit cell; $Z=3$ for $m=$ odd, $Z=$ 2 for $m=$ even). $\mathrm{In}_{1-x} \mathrm{Fe}_{1+x} \mathrm{O}_{3}(\mathrm{ZnO})_{m}$ (the value of $x$ for each $m$ is given in the last column of Table II) is consisted of $Z * 1$ $\left(\mathrm{In}_{1-x} \mathrm{Fe}_{x}\right) \mathrm{O}_{1.5}, Z * 1(\mathrm{FeZn}) \mathrm{O}_{2.5}$, and $Z *(m$ -1) ZnO layers.

## Experimental

$\mathrm{In}_{2} \mathrm{O}_{3}(99.9 \%), \mathrm{Fe}_{2} \mathrm{O}_{3}(99.99 \%)$, and ZnO ( $99.99 \%$ ) were used as starting compounds. Prior to mixing, $\mathrm{In}_{2} \mathrm{O}_{3}$ was heated at $800^{\circ} \mathrm{C}$ for one day, ZnO at $1000^{\circ} \mathrm{C}$ for half a day, and $\mathrm{Fe}_{2} \mathrm{O}_{3}$ at $1000^{\circ} \mathrm{C}$ for one day. Calculated amounts of the starting compounds were weighed and thoroughly mixed in an agate mortar under ethyl alcohol. Each of the mixtures was sealed in a Pt tube and heated in a vertical quench furnace with a

SiC heating element. The temperature was maintained at $1350 \pm 3^{\circ} \mathrm{C}$ by a PID electronic controller. After heat treatment, the samples were rapidly cooled to room temperature, and supplied to X-ray powder diffractometry for phase identification and measurement of the lattice constants. The samples were heated successively until equilibrium was obtained. It was considered that equilibrium was attained when the X-ray powder diffraction pattern of a specimen showed no change with successive heat treatment of the specimen. In order to ascertain whether the equilibrium states in the ternary system were reached or not, we heated some of mixtures containing binary compounds and/or ternary compounds which were prepared from the starting compounds, besides heating the mixture composed of $\mathrm{In}_{2} \mathrm{O}_{3}, \mathrm{Fe}_{2} \mathrm{O}_{3}$, and ZnO . We obtained the same phase assemblages from different starting mixtures with the same chemical compositions. Lattice constants were calculated by means of the leastsquares method. When the samples were obtained in single phase states, we estimated the stoichiometry from the mixing ratio of the starting compounds. Before and after each heat treatment, the weights of the tubes including the samples were measured. No evaporation of the samples could be detected in the process of heat treatment. Although chemical reaction between the Pt tube and the samples were checked visually, no detectable reaction was observed. Some of the samples obtained were supplied for SEM and high resolution electron microscopy in order to observe the morphology and the lattice images for the layered compounds.

## Results and Discussion

(I) The Phase Relations in the
$\mathrm{In}_{2} \mathrm{O}_{3}-\mathrm{Fe}_{2} \mathrm{ZnO}_{4}-\mathrm{ZnO}$ System at $1350^{\circ} \mathrm{C}$
The phase relations in the $\mathrm{In}_{2} \mathrm{O}_{3}-$ $\mathrm{Fe}_{2} \mathrm{ZnO}_{4}-\mathrm{ZnO}$ system at $1350^{\circ} \mathrm{C}$ are shown


Fig. 1. The phase relations in the $\mathrm{In}_{2} \mathrm{O}_{3}-\mathrm{Fe}_{2} \mathrm{ZnO}_{4}-\mathrm{ZnO}$ system at $1350^{\circ} \mathrm{C}$. Symbols and numbers in the figure are as follows; $\mathrm{A}_{1}:(0.320,0.180,0.500), \mathrm{A}_{2}:(0.250,0.250,0.500), \mathrm{A}_{3}:(0.100,0.400,0.500)$, $\mathrm{A}_{4}:(0.064,0.436,0.500), \mathrm{A}_{5}:(0.041,0.459,0.500), \mathrm{A}_{6}:(0.026,0.474,0.500), \mathrm{A}_{7}:(0.021,0.479,0.500)$, $A_{8}:\left(\right.$ undetermined), $A_{9}:(0.011,0.489,0.500) . B_{1}:(0.282,0.051,0.667), B_{2}:(0.214,0.119,0.667)$, $B_{3}:(0.160,0.173,0.667), B_{4}:(0.141,0.192,0.667) . C_{1}:(0.250,0.000,0.750), C_{2}:(0.212,0.038,0.750)$, $\mathrm{C}_{3}:(0.111,0.139,0.750), \mathrm{C}_{4}:(0.084,0.166,0.750) . \mathrm{D}_{1}:(0.200,0.000,0.800), \mathrm{D}_{2}:(0.080,0.120,0.800)$, $\mathrm{D}_{3}:(0.062,0.138,0.800) . \mathrm{E}_{1}:(0.167,0.000,0.833), \mathrm{E}_{2}:(0.056,0.111,0.833), \mathrm{E}_{3}:(0.041,0.126,0.833)$. $\mathrm{F}_{1}:(0.143,0.000,0.857), \mathrm{F}_{2}:(0.043-0.030,0.100-0.113,0.857), \mathrm{F}_{3}$ : (between $\mathrm{F}_{2}$ and $\left.0.030,0.113,0.857\right)$. $\mathrm{G}_{1}:(0.125,0.000,0.875), \mathrm{G}_{2}:(0.031,0.094,0.875) . \mathrm{H}_{1}:(0.111,0.000,0.889), \mathrm{H}_{2}:(0.031-0.020,0.080-$ $0.091,0.889) . \mathrm{I}_{1}:(0.100,0.000,0.900), \mathrm{I}_{2}:(0.010,0.090,0.900) . \mathrm{J}_{1}:(0.091,0.000,0.909), \mathrm{J}_{2}:(0.011-0.005$, $0.079-0.086,0.909) . \mathrm{K}_{1}:(0.083,0.000,0.917), \mathrm{K}_{2}:(0.017-0.000,0.066-0.083,0.917) . \mathrm{L}_{1}:(0.077,0.000$, $0.923), \mathrm{L}_{2}:(0.000,0.077,0.923) . \mathrm{M}_{1}:(0.071,0.000,0.929), \mathrm{M}_{2}:(0.000,0.071,0.929) . \mathrm{N}_{\mathrm{t}}:(0.080,0.480$, 0.440 ).
in Fig. 1. Mixing ratio of the starting compounds, heating periods, and phases obtained for establishing the phase relations in
the present system are shown in Tables $\mathrm{I}(\mathrm{A})$ and $\mathrm{I}(\mathrm{B})$. In the $\mathrm{In}_{2} \mathrm{O}_{3}-\mathrm{ZnO}$ system, there exist homologous binary phases, $\mathrm{In}_{2}$


Fig. 1-Continued
$\mathrm{O}_{3}(\mathrm{ZnO})_{m}(m=3-13)$, which are isostructural with $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{m}$. Kasper (6) originally prepared $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{m}$ in air at elevated temperatures and reported the lattice constants of the samples obtained under the conditions of synthesis. Cannard and Tilley (7) concluded from the lattice images for $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{m}$ by a high resolution electron microscopy that the structures having the layered structures are composed of $\mathrm{InO}_{1.5}$ and ZnO layers. We could not observe $\mathrm{In}_{2}$ $\mathrm{O}_{3}(\mathrm{ZnO})_{m}(m=1$ and 2$)$ at $1350^{\circ} \mathrm{C}$. The reaction rate of formation for $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{m}$ ( $m=$ even) from both $\mathrm{In}_{2} \mathrm{O}_{3}$ and ZnO powders were much slower than that of $\mathrm{In}_{2} \mathrm{O}_{3}$ $(\mathrm{ZnO})_{m}(m=$ odd $)$. Although $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{m}$ ( $3 \leqq m \leqq 13$ ) is clearly identified by means of powder $X$-ray diffractometry, $\quad \mathrm{In}_{2} \mathrm{O}_{3}$ $(\mathrm{ZnO})_{m}(m \geqq I 4)$ heated at $1350^{\circ} \mathrm{C}$ could not be identified, because X-ray powder diffraction peaks were too broad. The phases obtained between $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{m}(m=13)$ and ZnO are different from both ZnO and
$\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{13}$, therefore it is clear that there should exist $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{m}(m \geqq 14)$ between ZnO and $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{13}$. A couple of mixtures in the $\mathrm{In}_{2} \mathrm{O}_{3}-\mathrm{ZnO}$ system were heated at $1550^{\circ} \mathrm{C}$ and the results are shown in Table $I(C)$. We did not explicitly describe the phases with $m \geqq 14$ in Fig. 1. However, we can guess from the viewpoint of the structural aspect that there should exist infinite numbers of phases to be described as $\mathrm{In}_{2} \mathrm{O}_{3}$ $(\mathrm{ZnO})_{m}$ between ZnO and $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{m}(m$ $=13)$. The crystallographic considerations to the phases of $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{m}$ will be described in Section II. The lattice constant of $\mathrm{In}_{2} \mathrm{O}_{3}$ phase in equilibrium with $\mathrm{In}_{2} \mathrm{O}_{3}$ $(\mathrm{ZnO})_{3}$ and that of the $\mathrm{In}_{2} \mathrm{O}_{3}$ in a single phase state are $a=1.011(1)(\mathrm{nm})$ and $a=$ 1.012(1) (nm) (JCPDS Card No. 6-416 shows $a=1.0118(\mathrm{~nm})$ ), respectively. We concluded that the $\mathrm{In}_{2} \mathrm{O}_{3}$ phase does not have a solid solution range in the direction to ZnO . The lattice constants of the $\mathrm{In}_{2} \mathrm{O}_{3}$ phase which is in equilibrium with various

TABLE I(A)
Mixing Ratio of the Starting Compounds $\left(\mathrm{In}_{2} \mathrm{O}_{3}, \mathrm{Fe}_{2} \mathrm{O}_{3}, \mathrm{ZnO}\right)$, Heating Period, and
Phases Obtained in the $\operatorname{In}_{2} \mathrm{O}_{3}-\mathrm{Fe}_{2} \mathrm{ZnO}_{4}-\mathrm{ZnO}$ System at $1350^{\circ} \mathrm{C}$

| Mixing ratio of starting compounds (in mole ratio) |  |  | Heating <br> Period (Day) | Phases and | their lattice constants (nm) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 0 | 1 | $3+3$ | $\mathrm{In}_{2} \mathrm{O}_{3}$ | $a=1.011(1)$ |
|  |  |  |  | III | $\begin{aligned} & a=0.3342(1) \\ & c=4.243 \quad(1) \end{aligned}$ |
| 1 | 0 | 1 | $3+3$ | $\mathrm{In}_{2} \mathrm{O}_{3}$ | $a=1.011$ (1) |
|  |  |  |  | III | $\begin{aligned} & a=0.3350(1) \\ & c=4.246 \quad(1) \end{aligned}$ |
| 16 | 9 | 25 | $3+8$ | I | $\begin{aligned} & a=0.3341(1) \\ & c=2.635(1) \end{aligned}$ |
| 27 | 23 | 50 | $7+3+4$ | I | $\begin{aligned} & a=0.3325(1) \\ & c=2.615 \end{aligned}$ |
| 1 | 1 | 2 | $3+3+4+3+8$ | I | $\begin{aligned} & a=0.3320(1) \\ & c=2.610(1) \end{aligned}$ |
| 37 | 3 | 80 | $3+8$ | $\mathrm{In}_{2} \mathrm{O}_{3}$ | $\mathrm{a}=1.011$ (1) |
|  |  |  |  | III | $\begin{aligned} & a=0.3341(1) \\ & c=4.229(1) \end{aligned}$ |
| 7 | 3 | 20 | $4+3$ | II | $\begin{aligned} & \mathrm{a}=0.3334(1) \\ & \mathrm{c}=2.278 \quad(1) \end{aligned}$ |
| 1 | 1 | 4 | $3+3$ | II | $\begin{aligned} & a=0.3309(1) \\ & c=2.258 \end{aligned}$ |
| 23 | 27 | 100 | $4+4$ | II | $\begin{aligned} & a=0.3301(1) \\ & c=2.257 \end{aligned}$ |
| 1 | 1 | 5 | $3+3$ | II | $\begin{aligned} & a=0.3306(1) \\ & c=2.258 \end{aligned}$ |
|  |  |  |  | III | $\begin{aligned} & \mathrm{a}=0.3298(1) \\ & \mathrm{c}=4.164 \end{aligned}$ |
| 1 | 0 | 3 | $3+7$ | III | $\begin{aligned} & a=0.3351(1) \\ & c=4.248 \quad(1) \end{aligned}$ |
| 4 | 1 | 15 | 3 | III | $\begin{aligned} & a=0.3322(1) \\ & c=4.210 \quad(1) \end{aligned}$ |
| 1 | 1 | 6 | $3+3$ | III | $\begin{aligned} & a=0.3299(1) \\ & c=4.166 \quad(1) \end{aligned}$ |
| 52 | 73 | 375 | 4+4 | III | $\begin{aligned} & a=0.3286(1) \\ & c=4.168 \end{aligned}$ |

TABLE (A)-Continued


TABLE I(A)-Continued


TABLE I(A)-_Continued


TABLE I(A)-Continued


TABLE I(A)—Continued


TABLE I(A)-Continued


TABLE I(A)-Continued


Note. The homologous phase with $m=1,2, \ldots$, or 13 in the $\operatorname{InFe} \mathrm{O}_{3}(\mathrm{ZnO})_{m}$ is defined as Phase-I, Phase-II,
or Phase-XIII. The lattice constants with $*$ could not be determined.

TABLE I(B)
Mixing Ratio of the Various Starting Phases, Heating Period, and Phases Obtained In the $\mathrm{In}_{2} \mathrm{O}_{3}-\mathrm{Fe}_{2} \mathrm{ZnO}_{4}-\mathrm{ZnO}$ System at $1350^{\circ} \mathrm{C}$

| Mixing ratio of starting phases (in mole ratio) | Heating Period (Day) |  | hases <br> and <br> lattice constants (nm) |
| :---: | :---: | :---: | :---: |
| $\begin{aligned} & \mathrm{InFeO}_{3}(\mathrm{ZnO})_{3}: \mathrm{InFeO}_{3}(\mathrm{ZnO})_{4}: \mathrm{Fe}_{2} \mathrm{ZnO}_{4} \\ & =8: 5: 7 \end{aligned}$ | $4+3$ | III | $\begin{aligned} & a=0.3283(1) \\ & c=4.171 \quad(1) \end{aligned}$ |
|  |  | spinel | $a=0.8483(1)$ |
| $\begin{aligned} & \mathrm{InFeO}_{3}\left(\mathrm{ZnO}_{4}: \mathrm{InFeO}_{3}\left(\mathrm{ZnO}_{5}: \mathrm{Fe}_{2} \mathrm{ZnO}_{4}\right.\right. \\ & \quad=5: 9: 6 \end{aligned}$ | $4+3$ | III | $\begin{aligned} & a=0.3279(1) \\ & c=4.174 \end{aligned}$ |
|  |  | IV | $\begin{aligned} & a=0.3277(1) \\ & c=3.301 \quad(1) \end{aligned}$ |
|  |  | spinel | $a=0.8477$ (1) |
| $\begin{aligned} & \mathrm{In}_{2} \mathrm{O}_{3}: \\ &= \mathrm{Fe}_{2} \mathrm{ZnO}_{4} \\ & 1\end{aligned}$ | 7 | $\mathrm{In}_{2} \mathrm{O}_{3}$ | $a=1.003(1)$ |
|  |  | I | $\mathrm{a}=0.3317$ (1) |
|  |  |  | $\mathrm{c}=2.607$ (1) |
|  |  | spinel | $a=0.8529(1)$ |
| $\begin{aligned} & \mathrm{InFeO}_{3}(\mathrm{Zn} 0) \\ & =11: \mathrm{ZnO} \\ & \quad 1: 1 \end{aligned}$ | 3 | IX | $\begin{aligned} & a=\# \\ & c=8.933 \end{aligned}$ |
|  |  | XI | $\begin{aligned} & a=0.3289(1) \\ & c=10.48 \quad(1) \end{aligned}$ |
|  |  | XII | $\begin{aligned} & a=* \\ & c=* \end{aligned}$ |
|  |  | XIII | $\begin{aligned} & a=* \\ & c=12.01 \quad(3) \end{aligned}$ |

Note. The homologous phase with $m=1,2, \ldots$, or 13 in the $\ln \mathrm{FeO}_{3}(\mathrm{ZnO})_{m}$ is defined as Phase-I, Phase-II, . . . , or Phase-XIII. The lattice constants with * could not be determined.
phases are shown in Fig. 2. In the $\mathrm{ZnO}-$ $\mathrm{Fe}_{2} \mathrm{ZnO}_{4}$ system there exist new binary phases. The reaction rate of formation for $\mathrm{Fe}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{m}$ from both $\mathrm{Fe}_{2} \mathrm{O}_{3}$ and ZnO powders is not so slow that we could obtain each of the single phases in the system. They seem to belong to a distorted wurtzite phase; however, they are eventually homologous phases with composition, $\mathrm{Fe}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{m}(m \geqq 12)$. The details of both
the chemical compositions and the structures for these phases will be given later. It was concluded that no solid solution of the spinel phase to the direction to ZnO phase exists, since no volume change of the unit cell was detected between stoichiometric $\mathrm{Fe}_{2} \mathrm{ZnO}_{4}$ in a single phase state and that in equilibrium with the $\mathrm{Fe}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{m}$ phase ( $m$ $=12$ ). The lattice constant of $\mathrm{Fe}_{2} \mathrm{ZnO}_{4}$ is $a$ $=0.8439(1)(\mathrm{nm})(J C P D S$ Card No. 22-1012

TABLE I(C)
Mixing Ratio of the Starting Compounds $\left(\mathrm{In}_{2} \mathrm{O}_{3}, \mathrm{Fe}_{2} \mathrm{O}_{3}, \mathrm{ZnO}\right)$, Heating Period, and Phases Obtained in the $\mathrm{In}_{2} \mathrm{O}_{3}-\mathrm{Fe}_{2} \mathrm{ZnO}_{4}-\mathrm{ZnO}$ System at $1550^{\circ} \mathrm{C}$


Note. The homologous phase with $m=1,2, \ldots$, or 13 in the $\operatorname{InFeO} \mathbf{O}_{3}(\mathrm{ZnO})_{m}$ is defined as Phase-I, Phase-II, . . . , or Phase-XIII. The lattice constants with $~ * ~ c o u l d ~ n o t ~ b e ~ d e t e r m i n e d . ~$
shows $a=0.84411(\mathrm{~nm})$ ). In the $\mathrm{Fe}_{2} \mathrm{ZnO}_{4}-$ $\mathrm{In}_{2} \mathrm{O}_{3}$ system, there exists no binary phase, but the ranges of solid solutions of both the spinel and $\mathrm{In}_{2} \mathrm{O}_{3}$ were observed from the volume changes of each unit cell. The solid solution of spinel phase was observed in the range between $\mathrm{Fe}_{2} \mathrm{ZnO}_{4}$ and $\mathrm{In}_{x} \mathrm{Fe}_{2-x} \mathrm{ZnO}_{4}$ $(x=0.40 \pm 0.02)$. The relation between the lattice constant and the concentration of $\mathrm{In}_{2} \mathrm{O}_{3}$ is shown in Fig. 3. Our main purpose
is in the area of the layered compounds, so we did not investigate the details of this spinel phase region so intensively as in the layered compounds area.

In the ternary $\mathrm{In}_{2} \mathrm{O}_{3}-\mathrm{Fe}_{2} \mathrm{ZnO}_{4}-\mathrm{ZnO}$ system, there exist $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{m}$ ( $m=$ integer) types of homologous solid solutions. In the case of $m=1$, the solid solution of $\mathrm{In}_{1+x} \mathrm{Fe}_{1-x} \mathrm{O}_{3}(\mathrm{ZnO})-\mathrm{InFeO}_{3}(\mathrm{ZnO})$ exists. In the case of $m=2$, the solid solution range
TABLE II
The Solid Solution Ranges of the Layered Phases, Lattice Constants, and Space Groups

| Phase | Temperature ( ${ }^{\circ} \mathrm{C}$ ) <br> Heating <br> Period (hour) <br> Crystal | Kasper(6) $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{\mathrm{m}}$ <br> Lattice constant(na) <br> Systea | Cannard and Tilley (I) <br> Tempera- <br> ture $\left({ }^{\circ} \mathrm{C}\right) \mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{\mathrm{m}}$ <br> Heating Lattice <br> Period constant(nm) <br> (day) | Kimizuka et al. (8) Temperature $\left.{ }^{\circ}{ }^{\circ} \mathrm{C}\right) \mathrm{InFeO}_{3}(\mathrm{ZnO})_{\text {m }}$ Heating Lattice Period constant(nm) (day) <br> Space Group | $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{\text {m }}$ Lattice constant(nm) | Present Hork olution range (a $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{\text {m }}$ Lattlee constant (nm) | $\begin{aligned} & \text { at } \left.1350^{\circ} \mathrm{C}\right) \\ & \mathrm{I}_{1}-\mathrm{Fe} \mathrm{e}_{1+\mathrm{x}} \mathrm{O}_{3}(\mathrm{ZnO})_{\text {II }} \\ & \text { Lattice } \\ & \text { constant(nm) } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I |  |  |  | 1300 $\mathrm{InFeO}_{3}(\mathrm{Zn} 0)$ <br> 6 $\mathrm{a}=0.3321(1)$ <br> R 3 m $\mathrm{c}=2.609(1)$ | $\begin{aligned} & \mathrm{In}_{1+\mathrm{x}} \mathrm{Fe}_{1-\mathrm{x}} \mathrm{O}_{3}(\mathrm{Zn} 0)(\mathrm{x}=0.28) \\ & \mathrm{a}=0.3341(1) \\ & \mathrm{c}=2.635(1) \end{aligned}$ | $\begin{aligned} & \mathrm{InFeO}_{3}(2 \mathrm{nO}) \\ & \mathrm{n}=0.3320(1) \\ & \mathrm{c}=\mathbf{2 . 6 1 0 ( 1 )} \end{aligned}$ |  |
| II | $\begin{gathered} 1550 \\ 2 \\ \text { Hex. } \end{gathered}$ | $\begin{aligned} & \mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{2} \\ & \mathrm{a}=0.3376(1) \\ & \mathrm{c}=2.3154(10) \end{aligned}$ |  | $\begin{array}{cl} 1300 & \mathrm{InFeO}_{3}(\mathrm{ZnO})_{2} \\ 13 & \mathrm{a}=0.3309(1) \\ \mathrm{P6}_{3} / \text { mac } & \mathrm{c}=2.257(1) \end{array}$ | $\begin{aligned} & \mathrm{In}_{1+x} \mathrm{Fe}_{1-\mathrm{x}} \mathrm{O}_{3}(\mathrm{Zn} 0)_{2}(\mathrm{x}=0.69) \\ & \mathrm{a}=0.3351(1) \\ & \mathrm{c}=2.295(1) \end{aligned}$ | $\begin{aligned} & \mathrm{InFcO}_{3}(\mathrm{ZnO})_{2} \\ & \mathrm{a}=0.3309(1) \\ & \mathrm{c}=2.258(1) \end{aligned}$ |  |
| III | $\begin{gathered} 1200 \\ 12 \\ \text { Rhom. } \end{gathered}$ | $\begin{aligned} & \mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{3} \\ & \mathrm{a}=0.3355(1) \\ & \mathrm{c}=4.2515(20) \end{aligned}$ |  | $\begin{array}{cl} 1450 & \mathrm{InFeO}_{3}(2 \mathrm{no})_{3} \\ 2 & \mathrm{a}=0.3300(1) \\ \mathrm{R} 3 \mathrm{~m} & \mathrm{c}=4.168(1) \end{array}$ | $\begin{aligned} & \mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{3} \\ & \mathrm{a}=0.3351(1) \\ & \mathrm{c}=4.248(1) \end{aligned}$ | $\begin{aligned} & \mathrm{InFeO}_{3}(2 n 0)_{3} \\ & \mathrm{a}=0.3299(1) \\ & \mathrm{c}=4.166(1) \end{aligned}$ | $\begin{aligned} & \mathrm{In}_{1-\mathrm{x}} \mathrm{Fe}_{1+\mathrm{x}_{3}}(\mathrm{ZnO})_{3}(\mathrm{x}=0.33) \\ & \mathrm{a}=0.3279(1) \\ & \mathrm{c}=4.174(1) \end{aligned}$ |
| IV | $\begin{gathered} 1200 \\ 50 \\ \text { Hex. } \end{gathered}$ | $\begin{aligned} & \mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{4} \\ & \mathrm{a}=0.3339(2) \\ & \mathrm{c}=3.352(2) \end{aligned}$ | ${ }_{3}^{1100} \mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{4}$ | $\begin{array}{cl} 1450 & \mathrm{InFeO}_{3}(\mathrm{ZnO})_{4} \\ 2 & \mathrm{a}=0.3294(1) \\ \mathrm{P6}_{3} / \text { mac } & \mathrm{c}=3.299(1) \end{array}$ | $\begin{aligned} & \mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{4} \\ & \mathrm{a}=0.3337(1) \\ & \mathrm{c}=3.353(1) \end{aligned}$ | $\begin{aligned} & \mathrm{InFeO}_{3}(2 \mathrm{n} 0)_{4} \\ & \mathrm{a}=0.3292(1) \\ & \mathrm{c}=3.298(1) \end{aligned}$ | $\begin{aligned} & \mathrm{In}_{1-\mathrm{x}} \mathrm{Fe}_{1+\mathrm{x}} \mathrm{O}_{3}(\mathrm{ZnO})_{4}(\mathrm{x}=0.38) \\ & \mathrm{a}=0.3260(1) \\ & \mathrm{c}=3.304(1) \end{aligned}$ |
| $v$ | $\begin{aligned} & 1050 \\ & 100 \\ & \text { Rhom. } \end{aligned}$ | $\begin{aligned} & 1 n_{2} \mathrm{o}_{3}(2 \mathrm{n} 0)_{5} \\ & \mathrm{a}=0.3327(1) \\ & c=5.8114(20) \end{aligned}$ | ${ }_{3}^{1.100} \mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{5}$ | $\begin{array}{cl} 1450 & \mathrm{InFeO}_{3}(\mathrm{ZnO})_{5} \\ 2 & \mathrm{a}=0.3288(1) \\ \mathrm{R} 5 \mathrm{~m} & \mathrm{c}=5.728(1) \end{array}$ | $\begin{aligned} & \mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{5} \\ & \mathrm{a}=0.3326(1) \\ & \mathrm{c}=5.810(1) \end{aligned}$ | $\begin{aligned} & \mathrm{InFeO}_{3}(\mathrm{ZnO})_{5} \\ & \mathrm{a}=0.32 \mathrm{~B} 7(1) \\ & \mathrm{c}=5.727(1) \end{aligned}$ | $\begin{aligned} & \mathrm{In}_{1-x} \mathrm{Fe}_{1+x} \mathrm{O}_{3}(\mathrm{ZnO})_{5}(x=0.51) \\ & \mathrm{a}=0.3260(1) \\ & \mathrm{c}=5.746(1) \end{aligned}$ |
| VI |  |  | ${ }_{3}^{1100} \mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{6}$ | $\begin{array}{cl} 1450 & \mathrm{InFeO}_{3}(\mathrm{ZnO})_{6} \\ 1 & \mathrm{a}=0.3283(1) \\ \mathrm{PG}_{3} / \mathrm{mmC} & \mathrm{c}=4.336(1) \end{array}$ | $\begin{aligned} & \mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{6} \\ & \mathrm{a}=0.3316(1) \\ & \mathrm{c}=4.394(1) \end{aligned}$ | $\begin{aligned} & \mathrm{InFeO}_{3}(\mathrm{ZnO})_{6} \\ & \mathrm{a}=0.3283(1) \\ & \mathrm{c}=4.339(1) \end{aligned}$ | $\operatorname{In}_{\substack{\mathrm{n}=* \\ \mathrm{c}=*}}$ |


| VII | $\begin{gathered} 1310 \\ 2 \\ \text { Rhor. } \end{gathered}$ | $\begin{aligned} & \mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{Zn} 0)_{7} \\ & \mathrm{~A}=0.3313(1) \\ & \mathrm{c}=7.362(4) \end{aligned}$ | $\begin{gathered} 1100 \\ 3 \end{gathered}$ | $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{7}$ | $\begin{gathered} 1450 \\ 2 \\ \text { RJam }^{2} \end{gathered}$ | $\begin{aligned} & \mathrm{InFeO}_{3}(2 \mathrm{nO})_{7} \\ & \mathrm{a}=0.3279(1) \\ & \mathrm{c}=7.285(1) \end{aligned}$ | $\begin{aligned} & \mathrm{In}_{2} \mathrm{O}_{3}(2 \mathrm{n} 0)_{7} \\ & \mathrm{a}=0.3310(1) \\ & \mathrm{c}=7.370(1) \end{aligned}$ | $\begin{aligned} & \mathrm{InFeO}_{3}(2 \mathrm{n} 0)_{7} \\ & \mathrm{a}=0.3279(1) \\ & \mathrm{c}=7.286(1) \end{aligned}$ | $\begin{aligned} & \mathrm{In}_{1-\mathrm{x}} \mathrm{Fe}_{1+\mathrm{x}^{\mathrm{O}}{ }_{3}(2 \mathrm{nO})_{7}(\mathrm{x}=0.50)}^{\mathrm{a}=0.3252(1)} \\ & \mathrm{c}=7.297(3) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| VIII |  |  |  |  | $\begin{gathered} 1450 \\ 7 \\ \mathrm{PG}_{3} / \mathrm{mmC} \end{gathered}$ | $\begin{aligned} & \mathrm{InFeO}_{3}(\mathrm{Zno})_{8} \\ & \mathrm{a}=0.3276(1) \\ & \mathrm{c}=5.375(1) \end{aligned}$ | $\begin{aligned} & \mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{Zn} 0)_{8} \\ & \mathrm{a}=0.3304(1) \\ & \mathrm{c}=5.432(1) \end{aligned}$ | $\begin{aligned} & \mathrm{InFeO}_{3}(\mathrm{ZnO})_{8} \\ & \mathrm{a}=* \\ & \mathrm{c}=5.374(17) \end{aligned}$ | $\begin{aligned} & \mathrm{In}_{1-x} \mathrm{Fe}_{1+x} \mathrm{O}_{3}(\mathrm{Zn} 0)_{B}(0.44 \leqq x \leq 0.64) \\ & c=* \end{aligned}$ |
| IX |  |  | $\begin{gathered} 1100 \\ 7 \end{gathered}$ | $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{3}$ | $\begin{gathered} 1450 \\ 3 \\ \text { RJm } \end{gathered}$ | $\begin{aligned} & \mathrm{InFeO}_{3}(\mathrm{ZnO})_{9} \\ & \mathrm{a}=0.3274(1) \\ & \mathrm{c}=8.841(1) \end{aligned}$ | $\begin{aligned} & \mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{9} \\ & \mathrm{a}=0.3299(1) \\ & \mathrm{c}=8.926(1) \end{aligned}$ | $\begin{aligned} & \mathrm{InFeO}_{3}(\mathrm{ZnO})_{\mathrm{g}} \\ & \mathrm{a}=0.3274(1) \\ & \mathrm{c}=8.843(1) \end{aligned}$ | $\begin{aligned} & \mathrm{In}_{1-\mathrm{x}} \mathrm{Fe}_{1+\mathrm{x}^{\mathrm{O}}}(\mathrm{ZnO})_{9}(x=0.80) \\ & \mathrm{a}=3.246(2) \\ & \mathrm{c}=8.840(7) \end{aligned}$ |
| x |  |  |  |  | $\begin{gathered} 1450 \\ 7 \\ \mathrm{PG}_{3} / \mathrm{mmc} \end{gathered}$ | $\begin{aligned} & \mathrm{InFeO}_{3}(\mathrm{ZnO})_{10} 10 \\ & \mathrm{a}=0.3272(1) \\ & \mathrm{c}=6.402(1) \end{aligned}$ | $\begin{aligned} & \mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{Zn} 0)_{10} \\ & a=\sharp \\ & \mathrm{c}=6.545(57) \end{aligned}$ | $\begin{aligned} & \mathrm{InFeO}_{3}(\mathrm{ZnO})_{10} \\ & a=* \\ & \mathrm{c}=6.427(69) \end{aligned}$ | $\mathrm{In}_{\substack{\mathrm{a}=* \\ \mathrm{c}=*}}^{\mathrm{IF}_{1+\mathrm{x}} \mathrm{O}_{3}(\mathrm{ZnO})_{10}(0.74 \leq \mathrm{x} \leq 0.89)}$ |
| XI |  |  | $\begin{gathered} 1100 \\ 3 \end{gathered}$ | $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{11}$ |  |  | $\begin{aligned} & \mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{Zn} 0)_{11} \\ & \mathrm{a}=0.3292(1) \\ & \mathrm{c}=10.49(1) \end{aligned}$ | $\begin{aligned} & \mathrm{InFeO}_{3}(\mathrm{ZnO})_{11} \\ & \mathrm{a}=0.3268(1) \\ & c=10.39(1) \end{aligned}$ | $\begin{aligned} & \mathrm{In}_{1-\mathrm{x}} \mathrm{Fe}_{1+\mathrm{x}} \mathrm{O}_{3}(2 \mathrm{nO}) 11(0.60<\mathrm{x}<1.00) \\ & \mathrm{c}=* \end{aligned}$ |
| XII |  |  |  |  |  |  | $\begin{aligned} & \mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{Zn} 0)_{12} \\ & \mathrm{a}=* \\ & \mathrm{c}=* \end{aligned}$ | $\begin{aligned} & \mathrm{InFeO}_{3}(\mathrm{ZnO})_{12} \\ & \mathrm{c}=\star \end{aligned}$ | $\begin{aligned} & \mathrm{Fe}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{12} \\ & \mathrm{a}=0.3243(2) \\ & \mathrm{c}=7.422(7) \end{aligned}$ |
| XIII |  |  |  |  |  |  | $\begin{aligned} & \mathrm{In}_{2} \mathrm{O}_{3}(2 \mathrm{n} 0)_{13} \\ & \mathrm{a}=0.3284(1) \\ & \mathrm{c}=12.04(1) \end{aligned}$ | $\begin{aligned} & \mathrm{InFeO}_{3}(2 \mathrm{nO})_{13}{ }^{3} \\ & \mathrm{a}=0.3269(2) \\ & \mathrm{c}=11.96(1) \end{aligned}$ | $\begin{aligned} & \mathrm{Fe}_{2} \mathrm{O}_{3}(2 \mathrm{nO})_{13} \\ & \mathrm{a}=0.3241(3) \\ & \mathrm{c}=11.91(1) \end{aligned}$ |

[^1]

Fig. 2. The lattice constants of $\mathrm{In}_{2} \mathrm{O}_{3}$ phase which is in equilibrium with various phases: (1) Phase-III, (2) Phase-I and Phase-II, (3) Phase-I, (4) Phase-I and spinel, (5) Phase-I and spinel, and (6) Phase-I and spinel.
of $\quad \mathrm{In}_{1+x} \mathrm{Fe}_{1-x} \mathrm{O}_{3}(\mathrm{ZnO})_{2}-\mathrm{InFeO}_{3}(\mathrm{ZnO})_{2}-$ $\mathrm{In}_{1-x} \mathrm{Fe}_{1+x} \mathrm{O}_{3}(\mathrm{ZnO})_{2}$ exists. In the case of $m=3$ to 7 , each of the solid solution ranges of $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{m}-\mathrm{InFeO}_{3}(\mathrm{ZnO})_{m}-\mathrm{In}_{1-x} \mathrm{Fe}_{1+x}$ $\mathrm{O}_{3}(\mathrm{ZnO})_{m}$ exists. The formation reaction of $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{m}(m=$ even $)$ is much slower than that of $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{m}(m=$ odd $)$ as in the binary system $\mathrm{In}_{2} \mathrm{O}_{3}-\mathrm{ZnO}$. The phases with $m=8,10$, and 12 (except $\mathrm{Fe}_{2} \mathrm{O}_{3}$ $\left.(\mathrm{ZnO})_{12}\right)$ could not be obtained as the single
phase state within our present experimental conditions; however, the quantity of these phases increased with increasing heating period. Therefore, we concluded that these phases should be stable. We could not present both the solid solution ranges and the lattice constants for these phases so correctly as in the experimental data for the case of $m=$ odd. In the case of phases with $m=12$ and 13 , the solid solutions range from $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{m}$ to $\mathrm{Fe}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{m}$ including $\quad \mathrm{InFeO}_{3}(\mathrm{ZnO})_{m}$. The solid solution ranges in each phase, the lattice constants and space group are listed in Table II together with the data reported by Kasper (6), Cannard and Tilley (7), and Kimizuka et al. (8). The characteristic features of the phase relations in the present ternary systems are summarized as follows. Phase-I is in equilibrium with $\mathrm{In}_{2} \mathrm{O}_{3}$, Phase-II, and spinel. Phase-II is in equilibrium with $\mathrm{In}_{2} \mathrm{O}_{3}$, Phase-I, Phase-III, and spinel. Phase-III is in equilibrium with $\mathrm{In}_{2} \mathrm{O}_{3}$, Phase-II, Phase-IV, and spinel. Phase-IV is in equilibrium with Phase-III, Phase-V, and spinel. Phase-V to Phase-XII have similar phase relations to Phase-IV. Phase-XIII or its higher order should be in equilibrium with two other homologous phases on both


Fig. 3. The lattice constants of $\mathrm{In}_{x} \mathrm{Fe}_{2-x} \mathrm{ZnO}_{4}$ with spinel structure $x=0-0.40$.
sides. $\mathrm{Fe}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{12}$ was obtained in PhaseXII; however, neither $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{12}$ nor In $\mathrm{FeO}_{3}(\mathrm{ZnO})_{12}$ was observed in a single phase state. $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{15}$ in Phase-XV was obtained at $1550^{\circ} \mathrm{C} . \mathrm{ZnO}$ is in equilibrium with a very high order homologous phase which we could not describe exactly here. Solid solutions of the layered phases with nonintegral $m$ could not be detected within our experimental conditions.
(II) Crystal Structural Consideration for the Homologous Solid Solution of $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{m}-\mathrm{InFeO}{ }_{3}(\mathrm{ZnO})_{m}-\mathrm{In}_{1-x}$ $\mathrm{Fe}_{1+x} \mathrm{O}_{3}(\mathrm{ZnO})_{m}(m=$ integer $)$
$\mathrm{InFeO}_{3}(\mathrm{ZnO})_{m}(m=1$ and 2$)$ obtained by solid state reactions from $\mathrm{In}_{2} \mathrm{O}_{3}, \mathrm{Fe}_{2} \mathrm{O}_{3}$, and ZnO powders at $1350^{\circ} \mathrm{C}$ were observed by SEM. We could see well-developed platelike single crystals. The lattice constants for the homologous solid solutions of the $\quad \mathbf{I n}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{m}-\mathrm{InFeO}_{3}(\mathrm{ZnO})_{m}-\mathrm{In}_{1-x}$ $\mathrm{Fe}_{1+x} \mathrm{O}_{3}(\mathrm{ZnO})_{m}$ are shown as a hexagonal system in Fig. 4.

Kimizuka et al. (8) reported that InFe $\mathrm{O}_{3}(\mathrm{ZnO})$ is isostructural with $\mathrm{YbFe}_{2} \mathrm{O}_{4}$ (3) composed of both $\mathrm{YbO}_{1.5}$ and $\mathrm{Fe}_{2} \mathrm{O}_{2.5}$ layers, and $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{m}$, of $\quad \mathrm{InO}_{1.5}$, $(\mathrm{FeZn}) \mathrm{O}_{2.5}$, and ZnO layers. The crystal structural models for the compounds In $\mathrm{FeO}_{3}(\mathrm{ZnO}) . \mathrm{InFeO}_{3}(\mathrm{ZnO})_{2}, \mathrm{InFeO}_{3}(\mathrm{ZnO})_{3}$, and $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{4}$ as the representatives in InFeO ${ }_{3}(\mathrm{ZnO})_{m}$ compounds are shown in Figs. 5A, 5B, 5C, and 5D, respectively. In $\mathrm{InFeO}_{3}(\mathrm{ZnO}), \mathrm{In}^{3+}$ ion is in the octahedral site, and both $\mathrm{Fe}^{3+}$ and $\mathrm{Zn}^{2+}$ ions are in the trigonal bipyramidal site. In $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{m}$ ( $m \geqq 2$ ), the In ion and both the Fe and Zn ions are located as in $\mathrm{InFeO}_{3}(\mathrm{ZnO})$, but additional Zn ions are in the tetrahedral site. These crystal structural models were concluded from the crystallographic consideration to $\left(\mathrm{YbFeO}_{3}\right)_{n} \mathrm{FeO}(n=1,2$, and 3) structures and the powder X-ray data of In$\mathrm{FeO}_{3}(\mathrm{ZnO})_{m}(m=1,2,3$, and 4) compounds (3-5, 10, and 11). From these crystal models, it is easy to understand the
relation between $a$ (or $c$ ) and the $\mathrm{Fe}_{2} \mathrm{O}_{3}$ concentration in the region between $\mathrm{In}_{2} \mathrm{O}_{3}$ $(\mathrm{ZnO})_{m}$ and $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{m}$. As shown in Fig. 4, the lattice constants $a$ and $c$ decrease with increasing $\mathrm{Fe}_{2} \mathrm{O}_{3}$ concentration. From the above consideration, therefore, in the $\mathrm{In}_{1+x} \mathrm{Fe}_{1-x} \mathrm{O}_{3}(\mathrm{ZnO})_{m}$ compounds, the Fe in $(\mathrm{FeZn}) \mathrm{O}_{2.5}$ layers is replaced by $\mathrm{In}^{3+}$ forming $\left(\mathrm{In}_{x} \mathrm{Fe}_{1-x} \mathrm{Zn}\right) \mathrm{O}_{2.5}$ layers. So the $\mathrm{In}_{1+x} \mathrm{Fe}_{1-x} \mathrm{O}_{3}(\mathrm{ZnO})_{m}$ compound should exist in $Z * 1$ pieces of $\operatorname{InO}_{1.5}$, $Z * 1\left(\mathrm{In}_{x} \mathrm{Fe}_{1-x} \mathrm{Zn}\right) \mathrm{O}_{2.5}$, and $Z *(m-1) \mathrm{ZnO}$ layers. So we can calculate the $c$ values from the following equation as already discussed in the literature (8),

$$
\begin{equation*}
C_{\mathrm{calcd}}=\{p+q+(m-1) * r\} * Z \tag{1}
\end{equation*}
$$

where $C_{\text {calcd }}(\mathrm{nm})$ is the thickness of the unit cell of the compounds, $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{m}$ or $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{m} . p$, thickness of $\mathrm{InO}_{1.5}$ layer $(\mathrm{nm}) ; q$, thickness of $(\mathrm{FeZn}) \mathrm{O}_{2.5}$ or $(\mathrm{InZn})$ $\mathrm{O}_{2.5}$ layer ( nm ); $r$, thickness of ZnO layer ( nm ) ; $\ell$, molecular number in a unit cell. We listed experimental values together with calculated values from the above equation in Tables $\operatorname{III}(\mathrm{A})$ and $\operatorname{III}(\mathrm{B})$, in which $(p+q)=0.8951(\mathrm{~nm})$ and $r=0.2602$ $(\mathrm{nm})$ were hypothetically used for $\mathrm{In}_{2} \mathrm{O}_{3}$ $(\mathrm{ZnO})_{m}$. In the case of $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{m}$, we could calculate $C_{\text {calcd }}(\mathrm{nm})$ in the same model using ( $p+q=0.8701(\mathrm{~nm})$ and $r=$ $0.2596(\mathrm{~nm})$. Note that $\left(\frac{1}{2}\right) \times(c=0.5207)$ $(\mathrm{nm})$ is equal to $0.2604(\mathrm{~nm})$, where $c$ means the lattice constant of ZnO (11). Also we show the relation between $c_{\text {obsd }} / z$ and $m$ in Figs. 6A and 6B. We can see a good linearity in them. In the region of the $\mathrm{InFeO}_{3}$ $(\mathrm{ZnO})_{m}-\mathrm{In}_{1-x} \mathrm{Fe}_{1+x} \mathrm{O}_{3}(\mathrm{ZnO})_{m}$, the $a$-axis decreases with increasing concentration of $\mathrm{Fe}^{3+}$, but slight change in the $c$-axis was actually observed (Fig. 4). In this region, the $\mathrm{In}^{3+}$ in the $\mathrm{InO}_{1.5}$ layer is replaced by $\mathrm{Fe}^{3+}$, forming the $\left(\mathrm{In}_{1-x} \mathrm{Fe}_{x}\right) \mathrm{O}_{1.5}$ layer. So there should exist $\left(\mathrm{In}_{1-x} \mathrm{Fe}_{x}\right) \mathrm{O}_{1.5},(\mathrm{FeZn}) \mathrm{O}_{2.5}$, and ZnO layers. When $\mathrm{In}^{3+}$ is partly substituted by $\mathrm{Fe}^{3+}$, the octahedron in which $\mathrm{In}^{3+}$


Fig. 4. The dependence of the hexagonal lattice constants ( $a$ and $c$ ) of the layered phases upon the $\mathrm{Fe}_{2} \mathrm{O}_{3}$ concentration. (A) Phase-I. (B) Phase-II. (C) Phase-III. (D) Phase-IV. (E) Phase-V. (F) PhaseVI. (G) Phase VII. (H) Phase-VIII. (I) Phase-IX. (J) Phase-X. (K) Phase-XI. (L) Phase-XII. (M) PhaseXIII.
centrally exists will be shrunk. This shrinkage effect upon the $a$-axis is clearly greater than that on the $c$-axis. The $a$ values for the compounds $\mathrm{Fe}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{m}$ were calculated based upon $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{m}$ type of crystal structures. We show the dependency of the $a$ upon the $m$ in Fig. 6C. We can see that all of the $a$ values approach the $a$ of wurtzite with increasing $m$ in $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{m}, \mathrm{InFeO}_{3}$
$(\mathrm{ZnO})_{m}$, and $\mathrm{Fe}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{m}$. From the dependence of both the $a$ and $c$ values upon the $\mathrm{Fe}^{3+}$ concentration in both $\mathrm{In}_{2} \mathrm{O}_{3}$ $(\mathrm{ZnO})_{m}-\mathrm{InFeO}_{3}(\mathrm{ZnO})_{m} \quad$ and $\mathrm{In}-$ $\mathrm{FeO}_{3}(\mathrm{ZnO})_{m}-\mathrm{In}_{1-x} \mathrm{Fe}_{1+x} \mathrm{O}_{3}(\mathrm{ZnO})_{m}$ regions, we can safely conclude that the crystal structural model for $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{m}$ composed of the stacking of $\mathrm{InO}_{1.5},(\mathrm{FeZn}) \mathrm{O}_{2.5}$, and ZnO layers is quite satisfactory. The


InFeO3(ZnO) 13


Fig. 5. The crystal structural models of $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{m}(m=1,2,3$, and 4). A, B, and C represent three kinds of triangular lattices. $M$ sites are occupied by Fe and/or Zn ions. ©, In ion; $\bullet, \mathrm{Fe}$ and/or Zn ion; $\mathrm{O}, \mathrm{O}$ ion.
structural analyses for single crystal of Lu $\mathrm{FeO}_{3}(\mathrm{ZnO})_{m}(m=1,4,5$, and 6$)$ which are isostructural with $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{m}$ are in progress by Isobe (12).

In conclusion, (i) there are a series of homologous solid solutions, $\operatorname{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{m}$ - In $\mathrm{FeO}_{3}(\mathrm{ZnO})_{m}-\mathrm{In}_{1-\lambda} \mathrm{Fe}_{1+\lambda} \mathrm{O}_{3}(\mathrm{ZnO})_{m}(m=1-$ 13) at $1350^{\circ} \mathrm{C}$, (ii) in the binary $\mathrm{ZnO}-\mathrm{Fe}_{2} \mathrm{O}_{3}$



Fig. 6. (A) The relation between $c_{\text {obsd }} / z$ and $m$ in $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{m}$. (B) The relation between $c_{\text {obsd }} / z$ and $m$ in $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{m}$. (C) The relation between $a$ and $m$ in $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{m}(\square, \square), \operatorname{InFeO}(\mathrm{ZnO})_{m}(\mathrm{O}, \Theta)$, and $\mathrm{Fe}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{m}(\boldsymbol{\Delta}) . \square$, Kasper (6); O, Kimizuka et al. (8); $\boldsymbol{\square}, \boldsymbol{\bullet}, \boldsymbol{\Delta}$, this work.
system, there should exist $\mathrm{Fe}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{m}$ ( $m$ $\geqq 12$ ) which are isostructural with In$\mathrm{FcO}_{3}(\mathrm{ZnO})_{m}$ at $1350^{\circ} \mathrm{C}$, and (iii) the crystal structures for the homologous solid solutions are composed of the $\mathrm{InO}_{1.5},\left(\mathrm{In}_{1-x} \mathrm{Fe}_{x}\right.$ $\mathrm{Zn}) \mathrm{O}_{2.5}$ and ZnO layers in the region of $\mathrm{In}_{2}$ $\mathrm{O}_{3}(\mathrm{ZnO})_{m}-\operatorname{InFeO}_{3}(\mathrm{ZnO})_{m}$, and $\left(\mathrm{In}_{1-x} \mathrm{Fe}_{x}\right)$ $\mathrm{O}_{1.5},(\mathrm{FeZn}) \mathrm{O}_{2.5}$, and ZnO layers in the region of the $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{m}-\mathrm{In}_{1-x} \mathrm{Fe}_{1+x}$
$\mathrm{O}_{3}(\mathrm{ZnO})_{m}$. We will report the detailed crystal structures of the phases in the vicinity of ZnO in the system $\mathrm{ZnO}-\mathrm{Fe}_{2} \mathrm{O}_{3}$ at $1350^{\circ} \mathrm{C}$ in the near future, and clarify whether the phases will be able to be identified by means of a distorted wurtzite structure or a series of homologous phases, $\mathrm{Fe}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{m}$ with $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{m}$-type structure ( $m=$ integer).

TABLE III(A)
$C_{\text {obsd }}(\mathrm{nm})$ and $C_{\text {calcd. }}(\mathrm{nm})$ FOR $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{m}$ COMPOUNDS

| Compound | $\mathrm{C}_{\text {obsd. }}$ (nm) | $\mathrm{C}_{\text {calked. }}$ (nm) | $\mathrm{C}_{\text {cobsul }}(\mathrm{nm})-\mathrm{C}_{\text {calcc. }}(\mathrm{nm})$ |
| :---: | :---: | :---: | :---: |
| $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})$ |  | 2.685 |  |
| $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{2}{ }^{(\underline{6})}$ | $2.3154(10) *$ | 2.311 | 0.0044 |
| $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{3}$ | 4.248 (1) | 4.247 | 0.001 |
| $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{4}$ | 3.353 (1) | 3.352 | 0.001 |
| $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{5}$ | 5.810 (1) | 5.808 | 0.002 |
| $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{6}$ | 4.394(1) | 4.393 | 0.001 |
| $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{7}$ | 7.370 (1) | 7.370 | 0.000 |
| $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{8}$ | $5.432(1)$ | 5.433 | -0.001 |
| $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{9}$ | 8.926(1) | 8.931 | -0.005 |
| $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO}){ }_{10}$ | $6.545(57) *$ | 6.474 | 0.071 |
| $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO}){ }_{11}$ | 10.49(1) | 10.49 | 0.00 |
| $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{12}$ |  | 7.515 |  |
| $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{13}$ | 12.04 (1) | 12.05 | $-0.01$ |
| $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO}){ }_{14}$ |  | 8.556 |  |
| $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{15}$ | 13.63(1) | 13.61 | 0.02 |
| $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO}){ }_{16}$ |  | 9.597 |  |
| $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO}){ }_{17}$ |  | 15.18 |  |
| $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{18}$ |  | 10.64 |  |
| $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO}) 19$ |  | 16.74 |  |
| $\mathrm{In}_{2} \mathrm{O}_{3}(\mathrm{ZnO})_{20}$ | 11.64(1)* | 11.68 | -0.04 |

Note. These data with * were not used for $C_{\text {calcd }}$.

TABLE III(B)
$C_{\text {obsd. }}(\mathrm{nm})$ and $C_{\text {calcd. }}(\mathrm{nm})$ FOR $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{m}$ Compounds

| Compound | $\mathrm{C}_{\text {obsd. }}$ ( nm ) | $\mathrm{C}_{\text {calcd. }}$ ( nm ) | $\mathrm{C}_{\text {obsd. }}(\mathrm{nm})-\mathrm{C}_{\text {calced. }}(\mathrm{nm})$ |
| :---: | :---: | :---: | :---: |
| $\mathrm{InFeO}_{3}(\mathrm{ZnO})$ | 2.610 (1) | 2.610 | 0.000 |
| $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{2}$ | 2.258 (1) | 2.259 | -0.001 |
| $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{3}$ | 4.166 (1) | 4.168 | -0.002 |
| $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{4}$ | 3.298 (1) | 3.298 | 0.000 |
| $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{5}$ | 5.727 (1) | 5.726 | 0.001 |
| $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{6}$ | 4.339 (1) | 4.336 | 0.003 |
| $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{7}$ | 7.286 (1) | 7.283 | 0.003 |
| $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{8}{ }^{(8)}$ | $5.375(1)^{*}$ | 5.375 | 0.000 |
| $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{9}$ | 8.843(1) | 8.841 | 0.002 |
| $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{10}{ }^{(\underline{8})}$ | $6.402(1)^{*}$ | 6.413 | -0.011 |
| $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{11}$ | 10.39(1) | 10.40 | -0.01 |
| $\mathrm{InFeO}_{3}(\mathrm{ZnO}) 12$ |  | 7.452 |  |
| $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{13}$ | 11.96(1) | 11.96 | 0.00 |
| $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{14}$ |  | 8.490 |  |
| $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{15}$ |  | 13.51 |  |
| $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{16}$ |  | 9.529 |  |
| $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{17}$ |  | 15.07 |  |
| $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{18}$ |  | 10.57 |  |
| $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{19}$ |  | 16.63 |  |
| $\mathrm{InFeO}_{3}(\mathrm{ZnO})_{20}$ | 11.61(2)* | 11.61 | 0.00 |

Note. These data with * were not used for $C_{\text {calcd }}$.

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[^1]:    Note. All of the lattice constants are given in the hexagonal crystal system. Hex., hexagonal; Rhom., rhombic. The lattice constants with $*$ could not be determined.

